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HST/FGS PARALLAXES OF AM CVN STARS AND ASTROPHYSICAL CONSEQUENCES*

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ABSTRACT

We present absolute parallaxes and relative proper motions for five AM CVn stars, which we obtained using the Fine Guidance Sensors on board the *Hubble Space Telescope*. Our parallax measurements translate into distances $d_{\text{AM CVn}} = 606^{+135}_{-93}$ pc; $d_{\text{HP Lib}} = 197^{+14}_{-12}$ pc; $d_{\text{CR Boo}} = 337^{+44}_{-35}$ pc; $d_{\text{V803 Cen}} = 347^{+32}_{-27}$ pc; and $d_{\text{GP Com}} = 75^{+2}_{-2}$ pc. From these distances we estimate the space density of AM CVn stars and suggest that previous estimates have been too high by about an order of magnitude. We also infer the mass accretion rates which allows us to constrain the masses of the donor stars, and we show that relatively massive, semi-degenerate donor stars are favored in all systems except GP Com. Finally, we give updated estimates for their gravitational-wave signals, relevant for future space missions such as the proposed *Laser Interferometer Space Antenna (LISA)*, based on their distances and the inferred masses of the binary components. We show that all systems but GP Com are excellent candidates for detection with *LISA*.

Subject headings: astrometry — interferometry — stars: distances — stars: individual (AM Canum Venaticorum, HP Librae, CR Bootis, V803 Centauri, GP Comae Berenices) — stars: cataclysmic variables

1. INTRODUCTION

The AM CVn stars are white dwarfs (WDs) accreting matter from a degenerate or semi-degenerate companion, constituted primarily of helium with traces of metals (but no hydrogen). Because of their evolved nature they exist in ultra-compact configurations, with orbital periods ranging from about one hour down to ten, possibly even five, minutes. General overviews of this class of ultra-compact binary stars are given by Warner (1995) and, more recently, Nelemans (2005).

The formation of AM CVn stars is as yet poorly understood, although several formation channels have been proposed to contribute significantly to the AM CVn population. The first is stable Roche-lobe overflow in a (formerly detached) double white dwarf binary, when the two white dwarfs are brought together by angular momentum loss due to the emission of gravitational waves (the WD channel; see Nelemans et al. 2001). The second is Roche-lobe overflow from a helium star onto a white dwarf, followed by a period minimum around ten minutes, caused by the quenching of helium fusion and the donor star becoming semi-degenerate – equivalent to the orbital period minimum in the hydrogen-rich Cataclysmic Variables (CVs) (the helium-star channel; e.g. Iben & Tutukov 1991; Nelemans et al. 2001). In

a third scenario, a hydrogen-main-sequence star starts mass transfer onto a white dwarf right at the time when its core is becoming depleted of hydrogen, shifting the normal CV orbital period minimum down to, again, about ten minutes depending on the level of hydrogen depletion (the evolved-CV channel; Podsiadlowski et al. 2003).

Determining which of these evolutionary channels actually produce AM CVn stars, and in what numbers, has been a long-standing problem. An important observable is the distance to known AM CVn stars: this helps in determining their space density, and their absolute magnitudes contain important information about the rate at which they accrete matter, which in turn constrains the masses of the donor stars.

In this paper we present *Hubble Space Telescope (HST)* parallaxes of five AM CVn stars, ranging from 17 to 46 minutes in orbital period. They were selected on their average V-band magnitude ($V < 16$) because of the source brightness limitations of the Fine Guidance Sensors (FGS). All five systems show quite characteristic accretion disk behavior. The shortest-orbital-period systems AM CVn and HP Lib, at 17 and 18 minutes respectively, have an apparently stable disk that appears optically thick with shallow helium absorption lines (e.g. Greenstein & Matthews 1957; O'Donoghue et al. 1994), while the longest-period system GP Com, at 46 minutes, has a stable disk that appears optically thin with strong helium emission lines (e.g. Nather et al. 1981). The two intermediate systems under consideration, CR Boo and V803 Cen at orbital periods of 24 and 27 minutes, display transitions between high and low accretion disk states, with the disk changing from absorption-line to emission-line states and the luminosity dropping by as much as five magnitudes (e.g. Wood et al. 1987; O'Donoghue et al. 1987). This is presumably caused by a thermal instability in their disks (Tsugawa & Osaki 1997). Photometrically, these AM CVn stars thus behave much like the

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well-studied CVs (e.g. Patterson et al. 1997, 2000).

The outline of this paper is as follows. We describe the observations and data reduction in Section 2, and present the parallaxes and absolute magnitudes in convenient tabular form in Section 3. We then discuss the implications of these results for the space density of AM CVn stars, for their mass accretion rates and the masses of the components, and for their gravitational-wave signals in Section 4.

2. OBSERVATIONS AND DATA REDUCTION

Ten sets of astrometric data were acquired with the Fine Guidance Sensors on board *HST* for each of our five science targets. At each epoch we measured several reference stars and the target multiple times to correct for intra-orbit drift. We obtained these sets in pairs typically separated by a week. Each complete data aggregate spans ~ 1.5 years, except for GP Com, where a servicing mission forced a one-year slip of an observation at one maximum parallax factor. Table 3 contains the epochs of observation and measured photometry for each AM CVn star. The data were reduced and calibrated as detailed in Benedict et al. (2002a, 2002b, 2005), McArthur et al. (2001), and Soderblom et al. (2005).

Because the parallaxes determined for the AM CVn stars have been measured with respect to reference frame stars which have their own parallaxes, we had to either apply a statistically derived correction from relative to absolute parallax (van Altena et al. 1995) or estimate the absolute parallaxes of the reference frame stars (listed in Table 4). We chose the second method, as it yields a more direct (less Galaxy-model dependent) way of determining the reference star absolute parallaxes.

In principle, the colors, spectral type, and luminosity class of a star can be used to estimate the absolute magnitude, M_V , and V -band absorption, A_V . The absolute parallax is then simply,

$$\pi_{\text{abs}} = 10^{-(V - M_V + 5 - A_V)/5} \quad (1)$$

To obtain the spectral type and luminosity class of all reference stars, we combined existing photometric data from the Two-Micron All Sky Survey (2MASS), proper motions from the USNO CCD Astrograph Catalog (UCAC2), and ground-based spectroscopic follow-up from the 2.5-m Isaac Newton Telescope (with IDS), the 4.2-m William Herschel Telescope (with ISIS), the 6.5-m Magellan-Baade telescope (with IMACS), and the FLWO 1.5-m (with FAST), where the acronyms in parentheses are the names of the spectrographs used. The spectra typically had a ~ 5 Å resolution and a wide spectral range, suitable for classification purposes from early- to late-type stars. Table 5 lists the spectral types and luminosity classes we obtained for our reference stars based on their independent photometric and spectroscopic classifications. Estimated classification uncertainties were used to obtain the errors on the $m - M$ values in that table.

Assuming an $R = 3.1$ Galactic reddening law (Savage & Mathis 1979), we derived A_V values by comparing the measured colors (Table 6) with intrinsic $(V - K)_0$ colors from Bessell & Brett (1988) and Cox (2000). The resulting A_V values are collected in Table 7, from which we calculated a field-wide average A_V to be used in Equation 1. The resulting reference star parallax estimations are listed in Table 5.

3. RESULTS

3.1. Parallaxes and Absolute Magnitudes

Table 1 lists the absolute parallaxes, proper motions, and absolute magnitudes we obtained for the five AM CVn stars. To determine the average absolute magnitudes, we first derived average values for the apparent magnitudes of our objects. AM CVn, HP Lib and GP Com have never been observed to show brightness variations much larger than about a tenth of a magnitude around their mean, and it is commonly assumed that their accretion disks are in stable states of high (AM CVn, HP Lib) or low (GP Com) mass transfer, such that the thermal instabilities that may trigger transitions between different brightness states do not occur. We could therefore use our accurate FGS photometry (Table 3), which consists of 10 visits per object well separated in time, to directly derive average apparent magnitudes for these three systems. The two other objects, V803 Cen and CR Boo, are known to show complex brightness variations, as also evidenced by our FGS photometry (Table 3). For these we used the results of extensive photometric monitoring campaigns conducted by Patterson et al. (1997, 2000) to estimate time-averaged apparent magnitudes, by simply averaging the flux levels reported for these systems over the multiple years of observations. For all systems, we have made the crucial assumption that the average flux levels at which they have been observed since their discovery are representative for their longer-term average flux levels. The results are collected in Table 1.

When using a trigonometric parallax to derive absolute magnitudes for a class of objects, a correction is usually made for the Lutz–Kelker (LK) bias (Lutz & Kelker 1973). This LK bias occurs when the number of stars in a population significantly increases (or decreases) with distance around the measured distance for a certain object in the population, both due to an increase in the sampled volume with distance and a decrease in the population space density with distance. This can be corrected for if one knows the scale height of the population under consideration. For the AM CVn stars, the scale height is not known and has to be estimated.

GP Com, together with its twin V396 Hya, quite likely belongs to a (potentially large) halo population of old and very metal-poor AM CVn stars (Marsh 1999; Morales-Rueda et al. 2003). For the shorter-period systems, we have no indication that they belong to a halo population. Significant amounts of metals have been detected in AM CVn, HP Lib and V803 Cen (Roelofs et al. 2006b,c), suggesting a thin or possibly thick disk origin. Similar data is as yet unavailable for CR Boo, but several more recently discovered AM CVn stars – SDSS J124058.03–015919.2 (Roelofs et al. 2005), and V406 Hya (Roelofs et al. 2006a) – show abundances of metals in optical spectra (typically Fe, Mg and Si) that are compatible with solar values. There is thus no evidence that the AM CVn stars in the solar neighborhood in general belong to a halo population. In addition, none of our objects show particularly large transverse velocities perpendicular to the Galactic Plane (see Table 1 for their proper motions). We thus assume that AM CVn, HP Lib, CR Boo and V803 Cen all belong to a disk population.

We model the space density of this population with a thin disk component of moderate age, with a scale height $h_{z,\text{thin}} = 300$ pc, plus an older thick disk component of scale height $h_{z,\text{thick}} = 1250$ pc that contributes 2% at $z = 0$ pc, where z is the distance from the Galactic Plane:

$$\frac{\rho(z)}{\rho(0)} = 0.98 \operatorname{sech}(z/300 \text{ pc}) + 0.02 \operatorname{sech}(z/1250 \text{ pc}) \quad (2)$$

We then calculate the LK bias $\Delta\pi$ numerically, as this allows for a relatively easy derivation of the LK bias correction (see below on how we apply this) for an arbitrarily complicated distribution of stars $\rho(\pi)$ by evaluating

$$\Delta\pi(\text{LK}) = \pi - \frac{\int \pi' d\pi' \frac{\rho(\pi')}{\pi'^4} \exp\left(-\frac{(\pi' - \pi)^2}{2\sigma_\pi^2}\right)}{\int d\pi' \frac{\rho(\pi')}{\pi'^4} \exp\left(-\frac{(\pi' - \pi)^2}{2\sigma_\pi^2}\right)} \quad (3)$$

where $\rho(\pi)$ will in general depend on the coordinates (but in our model population, only on the Galactic latitude) of the object under study, and the $\pi^{-4}d\pi$ term is simply the increase in (phase) space with π . We perform this convolution integral between $\pi \pm 5\sigma_\pi$; for parallax measurements with $\sigma_\pi/\pi \geq 0.2$, an LK bias correction will become increasingly unrealistic (e.g. Lutz & Kelker 1973), although in our case the decreasing $\rho(\pi)$ with $\pi \rightarrow 0$ due to the finite population scale height keeps the integral well-behaved. The fact that our sample is, essentially, magnitude limited, causes an additional suppression of the population density $\rho(\pi)$ towards $\pi \rightarrow 0$ (e.g. Smith 2003; also Lutz & Kelker 1973). However, the object for which this potentially matters due to its relatively large measurement error (i.e. AM CVn; $\sigma_\pi/\pi = 0.18$) is at high Galactic latitude such that the assumed finite scale height has already effectively killed off the population $\rho(\pi)$ at small π .

GP Com, for which we assumed a halo origin, essentially represents the limiting case $\rho(\pi) \rightarrow \text{constant}$ since its observed distance is much smaller than any reasonable choice of scale height for the halo.

The resulting LK bias corrections on the absolute magnitudes, $\Delta M(\text{LK})$, are given in Table 1. We have used them to convert the inferred absolute magnitude for e.g. AM CVn, based on its measured distance, to the average absolute magnitude that a *sample of objects exactly like AM CVn* would have:

$$M_V = \langle V \rangle - (m - M) - A_V + \Delta M(\text{LK}) \quad (4)$$

That is, we apply the LK bias correction to the M_V 's of the individual objects in our sample. In practice, these $\Delta M(\text{LK})$'s are actually quite small compared to the 'raw' measurement uncertainties in the distance moduli $m - M$. The errors on these corrections, also given in Table 1, have been estimated by varying the modeled thin disk scale height from 200–500 pc. All results, including the final absolute magnitudes we obtain for the five stars, are listed in Table 1.

4. DISCUSSION

4.1. Previous Distance Measurements

4.1.1. Ground-based parallax measurements

Two of our targets (AM CVn and GP Com), as well as one other member of the AM CVn class (V396 Hya) have a measured ground-based parallax. Thorstensen (2003)

derived a parallax for GP Com of 14.8 ± 1.3 mas, translating into a distance of 68_{-6}^{+7} pc, in good agreement with our determination. For V396 Hya, J. R. Thorstensen (private communication) derives a parallax of 12.9 ± 1.4 mas, translating into a distance of 76_{-8}^{+11} pc, very close to the distance found for GP Com.

A ground-based absolute parallax of 4.25 ± 0.43 mas is derived for AM CVn itself (C. Dahn 2004, as quoted by Nelemans et al. 2004), translating into a distance of 235 pc. This is in disagreement with our measurement at the 5- σ level. The origin of this rather significant discrepancy is not clear. We have no reason to question the FGS measurements, but we do note that there were only three suitable reference stars in the field of AM CVn, whereas we used five for the other sources. This makes AM CVn's measurement more susceptible to errors in the reference star grid. On the other hand, if AM CVn really were at 235 pc, it seems highly unlikely that we should not have detected a much larger signal.

None of the other AM CVn stars have a ground-based parallax determination so far. A lower limit to the distance to CR Boo is set by C. Dahn (2004, as quoted by Espaillat et al. 2005) of $d_{\text{CR Boo}} > 250$ pc, fully consistent with our measurement.

4.1.2. Model-based distances

A number of accretion disk modeling studies have been done, where the observed optical spectra, in particular the shapes of the spectral lines and the overall slope of the spectrum, are fitted to accretion disk models to derive a number of parameters, including the distance. Estimates include: $d_{\text{ES Cet}} = 350$ pc (Espaillat et al. 2005); $d_{\text{CR Boo}} = 469 \pm 50$ pc, $d_{\text{HP Lib}} = 188 \pm 50$ pc, $d_{\text{V803 Cen}} = 405 \pm 50$ pc, $d_{\text{AM CVn}} = 288 \pm 50$ pc (all from Nasser et al. 2001); and $d_{\text{AM CVn}} = 420 \pm 80$ pc, $d_{\text{CR Boo}} = 206 \pm 15$ pc (El-Khoury & Wickramasinghe 2000).

Comparing these values with our parallaxes, the large discrepancy with the distance to AM CVn is again striking, whereas the values for CR Boo scatter around our parallax value, and the determination for HP Lib is dead-on target. The different model predictions for AM CVn and CR Boo differ quite a bit, the difference being formally significant at the 5- σ level for CR Boo.

Based on our *HST/FGS* parallaxes, it would thus appear that ground-based parallaxes up to at least 75 pc can give quite reliable results, whereas ground-based parallaxes at several hundred pc as well as distances obtained from disk modeling remain uncertain.

4.2. Space Density of AM CVn Stars

Based on an estimated $M_V = 9.5$ for the AM CVn stars in their high states, and the resulting distances $d < 100$ pc for five of the six AM CVn stars known at the time, Warner (1995) derived a local space density $\rho(0) \sim 3 \times 10^{-6} \text{ pc}^{-3}$ for the systems that are (mostly) in a high state.

Our *HST* parallaxes show that the absolute magnitude in the high states is close to $M_V = 6$, significantly brighter than the value used by Warner (1995). Despite the increase in the number of known AM CVn stars in recent years, mainly due to the Sloan Digital Sky Survey (Anderson et al. 2005; Roelofs et al. 2005), the number

TABLE 1
AM CVN PARALLAXES, PROPER MOTIONS, AND ABSOLUTE MAGNITUDES

Parameter	AM CVn	HP Lib	CR Boo	V803 Cen	GP Com
Study Duration (yr)	1.59	1.53	1.62	1.51	2.4
Observation Sets (#)	10	10	9	10	10
Reference stars (#)	3	5	5	5	5
Reference stars $\langle V \rangle$	13.98	13.18	12.09	14.58	14.50
Reference stars $\langle B - V \rangle$	0.84	0.75	0.81	0.67	0.80
HST π_{abs} (mas)	1.65 ± 0.30	5.07 ± 0.33	2.97 ± 0.34	2.88 ± 0.24	13.34 ± 0.33
HST relative μ (mas yr $^{-1}$)	34.25 ± 0.88	33.59 ± 1.54	38.80 ± 1.78	9.94 ± 2.98	352.36 ± 12.79
in Position Angle ($^{\circ}$)	67.0 ± 1.7	314 ± 14	-79.9 ± 3.7	248 ± 11	-84.7 ± 3.1
d (pc)	606^{+135}_{-93}	197^{+14}_{-12}	337^{+44}_{-35}	347^{+32}_{-27}	75^{+2}_{-2}
$\langle V \rangle$	14.02 ± 0.05	13.59 ± 0.05	14.5 ± 0.2	14.0 ± 0.2	15.94 ± 0.05
A_V	0.05 ± 0.02	0.34 ± 0.06	0.03 ± 0.04	0.31 ± 0.09	0.02 ± 0.11
$m - M$	$8.91^{+0.44}_{-0.36}$	$6.47^{+0.15}_{-0.14}$	$7.64^{+0.26}_{-0.24}$	$7.70^{+0.19}_{-0.17}$	$4.37^{+0.05}_{-0.05}$
LK bias ΔM	-0.16 ± 0.05	-0.03 ± 0.00	-0.09 ± 0.01	-0.06 ± 0.00	-0.01 ± 0.00
M_V	$4.90^{+0.37}_{-0.45}$	$6.75^{+0.16}_{-0.17}$	$6.74^{+0.32}_{-0.33}$	$5.93^{+0.28}_{-0.29}$	$11.54^{+0.13}_{-0.13}$

of known systems that have high states of $m_V \leq 14.5$ is still four. It would thus seem that we can lower the estimates by Warner (1995) that were based on this sample. We employ the “ $1/V_{\text{max}}$ ” method of Schmidt (1975), generalized to include the variation of space density with Galactic height:

$$\rho(0) = \frac{1}{4\pi\beta} \sum_{\text{obj}} \frac{1}{\int_0^{r_{\text{max}}} r^2 dr \rho(z)/\rho(0)} \quad (5)$$

Here r_{max} is the maximum distance at which an object would still just belong to the sample at $m_V = 14.5$ given its M_V , and $0 < \beta \leq 1$ is an (unknown) completeness parameter that corrects for the systems that would have belonged to our sample had they been discovered. The decrease in space density with Galactic height $z = r \sin b$, i.e. the term $\rho(z)/\rho(0)$, is modeled as in Section 3.1 (Eq. (2)). Summing over the four known objects in our sample then leads to a local space density of $\rho(0) = 2 \times 10^{-8} \beta^{-1} \text{ pc}^{-3}$ for the short-period AM CVns that have high states. Assuming a sample completeness β of only 10%, based on the notion that there are still large parts of the sky such as the Galactic Plane that are poorly surveyed, our result is still an order of magnitude lower than Warner’s (1995) estimate for this population.

If we combine the above result with the notion that AM CVn stars with orbital periods $P_{\text{orb}} \lesssim 2000$ s are observed to be in a high state at least some of the time, and we compare with evolutionary predictions that only about 2% of the local AM CVn population should currently be at these or shorter orbital periods (Nelemans et al. 2001, 2004), we arrive at a local space density estimate

$$\rho(0) \approx 1 \times 10^{-6} \beta^{-1} \text{ pc}^{-3} \quad (6)$$

for the entire AM CVn population, including the old and dim ones at long orbital periods.

If we again allow for a sample completeness β of only 10%, our space density for the entire population is still an order of magnitude lower than predictions from population synthesis models by Nelemans et al. (2001, 2004), which indicate $\rho(0) \sim 1 \times 10^{-4} \text{ pc}^{-3}$ (there is a small dependency of our ‘observed’ space density on the population models, because the 2% fraction of systems at $P_{\text{orb}} < 2000$ s was derived from them). It thus appears

that space density estimates – both of the bright, short-period ones and of the entire population – have so far been too high by about an order of magnitude. The sample completeness estimate β is nevertheless still very uncertain, and a more homogeneous sample of AM CVn stars will be needed to bring down the corresponding uncertainty in the space density (Roelofs et al. 2007b).

4.3. Mass Accretion Rates

From the absolute magnitudes we can estimate the mass accretion rates, \dot{M} , in our AM CVn stars, assuming that the observed flux is dominated by the accretion luminosity. For this we need to estimate what fraction of the total accretion luminosity of the stars is emitted in the V band; that is, we need the bolometric correction.

To determine this correction, we compose the spectral energy distributions (SEDs) for all systems except GP Com, based on the optical fluxes, archival *IUE* spectra covering the far- and near-UV, and their 2MASS detections. See Figure 1. The most reliable SEDs are those of the non-outbursting systems AM CVn and HP Lib; that of AM CVn has the additional advantage that the extinction towards AM CVn is low thanks to its high Galactic latitude, reducing the impact of uncertainties in the extinction correction. We see that the slopes of the UV spectra suggest at least ~ 30 kK ‘blackbody’ components, although both in the infrared and at the far-UV end of the spectra there is a flux excess relative to a 30 kK blackbody, indicating that the systems are not described perfectly by a single-temperature blackbody. At the far-UV end, we could be seeing a contribution from the accreting white dwarf, which is expected to have an effective temperature of ~ 40 kK (Bildsten et al. 2006). However, this contribution to the UV flux has to be small since the quiescent magnitudes of V803 Cen and CR Boo indicate that the accretor contributes no more than a few per cent of the light in the optical, while the accretor is not expected to be much hotter than the disk. The donor star is expected to have an effective temperature of only a few thousand Kelvin (C. Deloye, private communication; Deloye et al. 2007), while it should not be larger than the disk; therefore it should not contribute significantly to the SED either. Thus we are most likely seeing a disk with a range of temperatures.

We first derive a *minimum* bolometric correction (BC) for AM CVn by summing all the *observed* fluxes, without extrapolating beyond the observed wavelengths. This yields a lower limit of $BC \leq -2.2$. We then have to estimate how much additional flux is beyond the observed wavelengths. By far the largest part of this flux will be at wavelengths shorter than the observed range. From the slopes of the far-UV spectra, which do not appear to be flattening off that much towards shorter wavelengths, we estimate that they continue as 30 kK blackbodies. With this estimated extra flux the total bolometric correction becomes $BC = -2.5 \pm 0.3$, where the error has been estimated by considering a 40 kK instead of a 30 kK blackbody. Given the similarity of the SEDs, we assume this bolometric correction for all systems (although CR Boo's *IUE* spectrum has a lower UV flux compared to its average optical flux, we assume that this is due to its outburst behavior).

The exception is GP Com, which is thought to be in a stable state of low mass transfer. Its SED has been shown to match rather well with a $T_{\text{eff}} = 11$ kK blackbody, which is expected to be the accreting white dwarf (Bildsten et al. 2006), plus helium emission lines from the accretion disk which appears optically thin in the continuum. We have therefore used a bolometric correction appropriate for an 11 ± 1 kK blackbody: $BC_{\text{GP Com}} = -0.5 \pm 0.2$. Since the temperature of the accreting white dwarf we see today is probably set by accretion heating that occurred a long time ago, when GP Com was a much shorter-period binary with much higher \dot{M} (Bildsten et al. 2006), we can only put an upper limit to GP Com's present-day accretion rate.

For a given system with a given BC, we can derive the bolometric luminosity, L , and compare with the value

$$L = \frac{1}{2} \dot{M}_2 (\Phi(L_1) - \Phi(R_1)) \quad (7)$$

expected for conservative mass transfer through a Keplerian (i.e. virialised) disk, where Φ is the Roche potential, at the inner Lagrange point L_1 and the surface of the accreting star R_1 . Since the accreting white dwarf is expected to be rather hot due to accretion-induced heating (Bildsten et al. 2006), at least for the four bright systems, we use accretor radii that are 5–10% (depending on mass) larger than the idealized zero-temperature radii, based on the mass-radius relations given by Panei et al. (2000). These correspond to a core temperature of about 3×10^7 K in the models of Bildsten et al. (2006, 2007).

We can then link the mass transfer rate to the component masses by assuming that gravitational-wave losses drive the evolution of the system, as is commonly assumed (e.g. Deloye et al. 2005; Marsh et al. 2004), and requiring that the secondary fill its Roche lobe. This gives an equilibrium mass transfer rate

$$\frac{\dot{M}_2}{M_2} = \frac{\dot{J}}{J} \frac{2}{\zeta_2 + 5/3 - 2q} \quad (8)$$

where the angular momentum loss due to the emission of gravitational waves is given by

$$\frac{\dot{J}}{J} = -\frac{32}{5} \frac{G^3}{c^5} \frac{M_1 M_2 (M_1 + M_2)}{a^4} \quad (9)$$

(Landau & Lifschitz 1971), $q \equiv M_2/M_1$ is the mass ratio of the binary, a is the separation between the donor mass

M_2 and the accretor mass M_1 , and

$$\zeta_2 \equiv \frac{d \log R_2}{d \log M_2}. \quad (10)$$

expresses the mass-radius relation of the mass-losing star. The latter may range from $\zeta_2 \approx -0.06$ for a semi-degenerate helium object based on evolutionary calculations by Tutukov & Fedorova (1989) as parameterized by Nelemans et al. (2001), to $\zeta_2 \approx -1/3$ for an (idealized) zero-temperature white dwarf.

For a given mass ratio q and a choice of mass-radius relation for the secondary star ζ_2 , the mass of the secondary M_2 is now fixed by the observed bolometric luminosity, if one makes the crucial assumption that the present-day accretion rate corresponds to the binary's equilibrium rate for gravitational-wave-driven mass transfer. At present only GP Com (Steeghs et al. in preparation) and AM CVn (Roelofs et al. 2006b) have a directly measured mass ratio; for the other three we can either estimate the primary's mass, or the mass ratio. In Roelofs et al. (2006b) we derive a primary mass $M_1 \approx 0.7 M_\odot$ for AM CVn, and combined with the mass distribution of single white dwarfs (e.g. Bergeron et al. 1992), it would seem reasonable to adopt a similar canonical white dwarf mass for the accretors in HP Lib, CR Boo, and V803 Cen.

We do, however, have one additional piece of information on these three systems: they all show 'superhump' periods (P_{sh}) in time-series photometry (e.g. Patterson et al. 1997, 2000, 2002), which are thought to be due to a tidal resonance between the accretion disk and the secondary star. Observationally and theoretically, it has been found that there exists a (roughly linear) relation between the superhump period excess ϵ , defined as

$$\epsilon \equiv \frac{P_{\text{sh}} - P_{\text{orb}}}{P_{\text{orb}}} \quad (11)$$

and the mass ratio q , at least for the hydrogen-rich Cataclysmic Variables (Patterson et al. 2005; Whitehurst 1988; Whitehurst & King 1991; Hirose & Osaki 1990). To date, there is only one AM CVn star for which we have both a kinematically derived mass ratio and a superhump period excess, namely AM CVn itself (Skillman et al. 1999; Roelofs et al. 2006b). We may estimate mass ratios for HP Lib, CR Boo, and V803 Cen by assuming a linear $\epsilon(q)$ relation,

$$\epsilon(q) = 0.12q \quad (12)$$

for them, based on $q = 0.18$, $\epsilon = 0.0218$ measured for AM CVn. The resulting mass ratios for HP Lib, CR Boo and V803 Cen are shown in Table 2. The first two of these are about twice as large as those used by Deloye et al. (2005), who employ an $\epsilon(q)$ relation that is based on fits to numerical simulations of accretion disks in hydrogen-rich CVs, as given by Warner (1995). Adopting instead the empirical $\epsilon(q)$ for hydrogen-rich CVs from Patterson et al. (2005) already yields larger mass ratios than the ones used in Deloye et al. (2005), but still smaller than ours. Our mass ratio estimate for V803 Cen is also much larger *relative* to the other systems than the one used by Deloye et al. (2005); this is due to a new robust measurement of V803 Cen's orbital period, as will be discussed in section 4.5. Although our $\epsilon(q)$ relation is uncertain since it is based solely on AM

CVn (see also Pearson 2007 for a recent discussion), it is probably the best we can do until independent mass ratio measurements become available for more AM CVn stars. We choose to employ this $\epsilon(q)$ relation combined with the known superhump excesses for HP Lib, CR Boo, and V803 Cen to estimate their individual mass ratios, rather than assume a canonical primary mass for all three.

Lastly, a correction has to be made for the inclination i of the binary, since the ‘apparent absolute magnitude’ (Warner 1995) depends on the inclination. We thus link the observed absolute magnitude M_V from Table 2 to the presumed accretion luminosity $M_{\text{bol}}(M_1, M_2)$ due to gravitational-wave radiation via

$$M_V = M_{\text{bol}}(M_1, M_2) - \text{BC} + \Delta M_V(i) \quad (13)$$

where

$$\Delta M_V(i) = -2.5 \log \left(\frac{\cos i}{0.5} \right) \quad (14)$$

is the correction due to the observer observing a different area of the disc than the direction-averaged value, $\langle \cos i \rangle = 0.5$ (the unknown effect of limb darkening is not taken into account). For HP Lib and V803 Cen the inclination is constrained by spectroscopic measurements of the velocity amplitude of the ‘bright spot’ (the presumed accretion stream–accretion disk impact region) in these systems (Roelofs et al. 2007a; see also section 4.5). We make the assumption that the radial velocity semi-amplitude of the donor star is equal to that of the bright spot, which is usually a good estimate. Similar data does not exist for CR Boo and we thus adopt the value of $i = 30^\circ$ derived from spectral line modeling by Nasser et al. (2001), with the sidenote that their model-derived inclinations for AM CVn, HP Lib, and V803 Cen are in excellent agreement with the kinematically derived values. Table 2 lists the inclinations we employ for all systems.

With the above assumptions we have all the ingredients needed to solve for the masses and mass transfer rates of our AM CVn stars: for a given mass ratio q , there is only one set of M_1 and M_2 for which the resulting accretion luminosity driven by gravitational-wave emission matches with the observed luminosity. For AM CVn, which has a kinematically measured mass ratio, the dominant contributions to the error on the mass transfer rate are the error on its absolute magnitude M_V and the uncertainty in the bolometric correction. For HP Lib, CR Boo, and V803 Cen, we consider the uncertainty on their true mass ratios to be the most important factor. The errors on the mass transfer rates for these systems are estimated by varying q by $\pm 50\%$ from the ‘best estimates’ given in Table 2. The resulting lower limits then correspond to the low mass ratios employed by Deloye et al. (2005), while the resulting upper limits correspond to q s that are such that $q_{\text{HP Lib}}$ coincides with our kinematically measured $q_{\text{AM CVn}}$, which one might expect if they share a similar evolutionary history, given their similar orbital period. Note that these ranges in q give ranges of M_2 and M_1 (see Table 2) that are anti-correlated. For GP Com, as mentioned, we can put upper limits on the accretion rate by assuming that the accretion luminosity has to be less than the observed luminosity (the latter of which is probably due in part to the accreting white dwarf). This leads to upper limits on $M_{1,2}$ under the

assumption that the mass transfer rate is set by the rate of gravitational-wave emission. The lower limits on $M_{1,2}$ correspond to the minimum mass a Roche-lobe-filling helium object can have at the observed orbital period of GP Com.

We can compare our values to those obtained by Nasser et al. (2001) from spectral modeling of the accretion disks in these systems. With our larger distance for AM CVn, the accretion rate based on their models should be a bit larger than our value, at $\dot{M}_{\text{AM CVn}} \sim 1 \times 10^{-8} M_\odot/\text{yr}$ (J.-E. Solheim, private communication). For the other systems they find $\dot{M} \sim 4 \times 10^{-9} M_\odot/\text{yr}$, which is again larger than our values of $\dot{M} \sim 1 \times 10^{-9} M_\odot/\text{yr}$. El-Khoury & Wickramasinghe (2000) on the other hand find $\dot{M}_{\text{AM CVn}} \sim 2 \times 10^{-9} M_\odot/\text{yr}$, also from spectral modeling of the accretion disk, which is lower than our value. Their value of $\dot{M}_{\text{CR Boo}} \sim 1 \times 10^{-9} M_\odot/\text{yr}$ is close to ours.

4.4. The Nature of the Donor Stars

The most surprising result of our *HST* parallaxes is the large distance to AM CVn, which exceeds every previous estimate. The resulting large luminosity of AM CVn already suggests a relatively high mass accretion rate. In addition to the large distance found here, AM CVn’s recently measured mass ratio, too, was found to be significantly larger than previously thought (Roelofs et al. 2006b). With these two pieces of information we could solve self-consistently for the masses of the components (within the assumptions outlined in Section 4.3), and provide strong evidence that the donor star in AM CVn is a relatively massive, semi-degenerate helium object.

For HP Lib, CR Boo, and V803 Cen, there is a larger uncertainty in the masses of the components due to the larger uncertainties on their mass ratios, as discussed in the previous section. Nevertheless, if we compare the data with evolutionary predictions for fully-degenerate and semi-degenerate donors (see Figure 2), the data are seen to favor rather massive, semi-degenerate donor stars in all systems but GP Com. This agrees qualitatively with the accretion disk models of Nasser et al. (2001), but disagrees with El-Khoury & Wickramasinghe (2000) who find a fully-degenerate donor in AM CVn.

It should be noted that there is a selection effect against fully-degenerate donor stars, since AM CVn stars with semi-degenerate donors are expected to be brighter at short orbital periods due to the higher mass accretion rates. At long orbital periods this is partially offset by the fact that semi-degenerate systems evolve to lower accretion rates more quickly. If we evolve a fully-degenerate and a semi-degenerate system, based on the parameterization of Nelemans et al. (2001), we see that semi-degenerate donors are in a bright state about twice as long, where we take ‘bright state’ to be $\dot{M}_2 \sim 10^{-8} - 10^{-10} M_\odot/\text{yr}$, i.e. a state corresponding to the four bright AM CVns under consideration here. See Figure 3.

We thus observe four relatively massive, semi-degenerate systems out of five, with a potential factor-of-two selection effect in favor of the semi-degenerates. We can conclude that at least a significant fraction, and possibly all, of the short-period systems (at $P_{\text{orb}} \lesssim 2000\text{s}$) have hot, semi-degenerate donors rather than

TABLE 2
APPARENT MASS ACCRETION RATES, INFERRED MASSES, AND GRAVITATIONAL-WAVE STRAIN AMPLITUDES

Parameter	AM CVn	HP Lib	CR Boo	V803 Cen	GP Com
P_{orb} (s)	1029	1103	1471	1596	2794
q	0.18 ^a	0.06 – 0.18 ^b	0.04 – 0.13 ^b	0.05 – 0.14 ^b	0.018 ^a
i (degrees)	43 ± 2	26 – 34	30 ^c	12 – 15	n/a
BC	−2.5 ± 0.3	−2.5 ± 0.3	−2.5 ± 0.3	−2.5 ± 0.3	−0.5 ± 0.2
\dot{M} ($M_{\odot} \text{ yr}^{-1}$)	7.1 ^{+2.2} _{−1.5} × 10 ^{−9}	[0.81 – 2.2] × 10 ^{−9}	[0.38 – 1.2] × 10 ^{−9}	[0.57 – 1.6] × 10 ^{−9}	< 3.6 ± 0.5 × 10 ^{−12}
M_2 (M_{\odot})	0.13 ± 0.01	0.048 – 0.088	0.044 – 0.088	0.059 – 0.109	0.009 – 0.012
M_1 (M_{\odot})	0.71 ± 0.07	0.80 – 0.49	1.10 – 0.67	1.17 – 0.78	0.50 – 0.68
L (W) ^d	2.2 ^{+1.4} _{−0.8} × 10 ²⁷	3.4 ^{+1.3} _{−0.9} × 10 ²⁶	3.5 ^{+1.2} _{−1.7} × 10 ²⁶	6.5 ^{+2.1} _{−3.1} × 10 ²⁶	< 1.1 ^{+0.3} _{−0.2} × 10 ²⁴
h	2.0 ^{+0.4} _{−0.3} × 10 ^{−22}	3.7 ^{+0.6} _{−0.8} × 10 ^{−22}	2.1 ^{+0.4} _{−0.5} × 10 ^{−22}	3.0 ^{+0.5} _{−0.7} × 10 ^{−22}	[4.0 – 6.6] × 10 ^{−23}

^a Measured from kinematics. ^b Inferred from superhump period; note the differences with Table 1 of Deloye et al. (2005). ^c From Nasser et al. (2001). ^d Inferred accretion luminosity, Eq. (7).

cold, degenerate ones. AM CVn stars with such hot, semi-degenerate donors are expected naturally from the helium-star channel (Nelemans et al. 2001), but a fraction of AM CVn progenitors in the WD channel are also expected to still have hot donors upon coming into contact (Deloye et al. 2005). Conceivably, it could be predominantly this hot fraction of systems that survive as AM CVn stars in the WD channel, since the mass transfer rate upon Roche-lobe overflow can be up to two orders of magnitude lower than for cold, degenerate donors (Nelemans et al. 2001; Deloye et al. 2005, 2007). Another possibility would be that cold white dwarf donors in the WD channel are reheated at some stage, for instance by tidal heating close to orbital period minimum (e.g. Iben et al. 1998) or in a thermonuclear event such as those proposed by Bildsten et al. (2007). Interpretation of our results in terms of the evolutionary history of the systems requires a more detailed study of these effects. Of particular interest would be a comparison between HP Lib and AM CVn, whose donor stars appear to have a different level of degeneracy despite their otherwise identical appearance (Roelofs et al. 2006b, 2007a). A kinematic measurement of HP Lib’s mass ratio would be needed to determine whether its donor star is truly more degenerate.

We remark that there is one, but really only one, crucial assumption in our analysis that leads us to conclude that the donor stars in AM CVns are semi-degenerate objects, namely, that the mass transfer rate is set by the emission of gravitational waves. If there should be an additional, dominant driver of mass transfer, we could be overestimating the masses enough (based on the observed luminosities) that the donors could in reality be fully degenerate. Within the assumption of gravitational-wave-driven mass transfer, the result that the donors are semi-degenerate is quite robust. This is a consequence of the accretion luminosity due to gravitational waves being strongly dependent on the masses of the stars, as can readily be judged from Eqs. (7)–(9). The uncertainty in the inferred masses is therefore small compared to the uncertainties in the bolometric luminosities of the systems.

The possibility of the mass transfer rate (due to gravitational waves) being out of equilibrium cannot be ruled out, but we do remark that it is quite difficult to change the donor star’s radius by for instance irradiation, since

the structure of the donor star is largely set by degeneracy pressure (C. Deloye, private communication). At late times ($P_{\text{orb}} \gtrsim 45$ min) a hot, semi-degenerate donor may start to cool and contract towards a fully-degenerate state, which could cause the mass transfer rate to go down temporarily (Deloye et al. 2007). This may be relevant for GP Com.

4.5. The Mass Ratio of V803 Cen

The small mass ratio of V803 Cen, $q_{\text{V803 Cen}} = 0.016$, implied by the small superhump period excess as obtained from Patterson (2001) by Deloye et al. (2005) and others, leads to a necessarily large accretor mass close to the Chandrasekhar limit, and a small donor mass close to the minimum mass for a Roche-lobe filling secondary (corresponding to a cold, fully-degenerate object). This was already noted by Deloye et al. (2005). Given these implications, it should be noted that V803 Cen is the one system for which the photometric superhump period excess appeared to be uncertain due to an uncertain identification of the 1611-second orbital period (see also Patterson et al. 2000), which has nevertheless entered the literature (Patterson 2001, Patterson et al. 2002, Woudt & Warner 2003, Deloye et al. 2005).

We have recently measured a significantly shorter orbital period, $P_{\text{V803 Cen}} = 1596.4 \pm 1.2$ seconds, from VLT spectroscopy (Roelofs et al. 2007a). The mass ratio we use in this paper is the one we obtain from the corresponding (larger) superhump period excess, via relation (12), again with a $\pm 50\%$ range. Since it is not completely clear whether the 1618s superhump period or the 1611s period (both from Patterson et al. 2000) is the more appropriate one to use for calculating the superhump period excess, we have used the average of the two.

The resulting mass ratio $q_{\text{V803 Cen}} = 0.05 - 0.14$ lifts the strong constraints on the mass of the donor (cf. Deloye et al. 2005). A semi-degenerate donor is then strongly favored, as shown in Section 4.3, and the accretor does not have to be very close to the Chandrasekhar mass in order to explain the observed luminosity of the system.

4.6. AM CVn Stars as Sources of Gravitational Waves

The ultra-compact nature of the AM CVn stars, combined with the relative proximity of the known systems, makes them the strongest known sources of gravitational

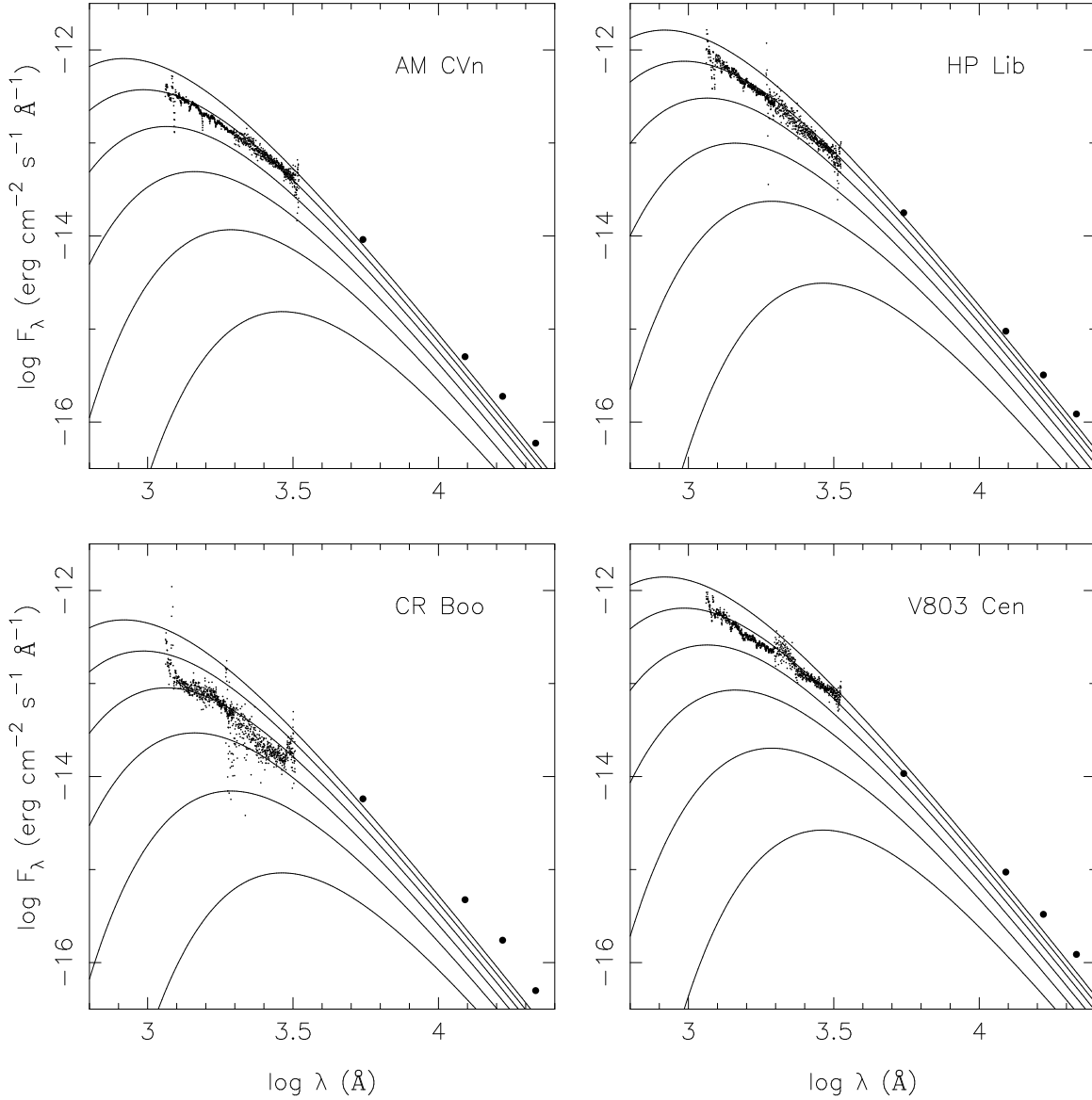


FIG. 1.— Observed spectral energy distributions of AM CVn, HP Lib, CR Boo, and V803 Cen, compiled from archival *IUE* spectra (small dots), the optical V-band fluxes from table 1 (left-most large dot), and the near-infrared J-, H-, and K-band fluxes from 2MASS (three right-most dots). The solid lines are blackbody spectra of $T_{\text{eff}} = 10 - 35$ kK in steps of 5 kK (bottom to top) to get an idea of the temperatures. For CR Boo and V803 Cen, we selected the apparent high-state spectra from the *IUE* archives; however, we cannot exclude that they represent slightly lower intermediate states. For CR Boo this was definitely the case for its short-wavelength (1150–2000 Å) spectrum; we scaled it up to match the overlapping long-wavelength (1850–3350 Å) *IUE* spectrum. Its UV flux still seems low with respect to the average optical flux and the 2MASS snapshots. The data have been corrected for extinction according to Cardelli et al. (1989) and assuming an $R_V = 3.1$ extinction law.

waves in the frequency regime covered by space-borne gravitational-wave detectors such as *LISA*.

The masses of the stars, inferred from their luminosities, can be used to estimate the gravitational-wave strain amplitudes of our five AM CVns. The gravitational-wave strain amplitude h is given by (see Roelofs et al. 2006b, after Timpano et al. 2006)

$$h = 2.84 \cdot 10^{-22} \sqrt{\cos^4 i + 6 \cos^2 i + 1} \times \left(\frac{\mathcal{M}}{M_\odot} \right)^{5/3} \left(\frac{P_{\text{orb}}}{1 \text{ hr}} \right)^{-2/3} \left(\frac{d}{1 \text{ kpc}} \right)^{-1} \quad (15)$$

where $\mathcal{M} = (M_1 M_2)^{3/5} / (M_1 + M_2)^{1/5}$ is the so-called chirp mass, and d the distance to the star. Figure 4 shows the resulting strain amplitudes of our five systems.

These values are quite insensitive to the uncertain mass ratios q of some of our systems; their errors are dominated by the errors on their bolometric luminosities. We see that the four short-period systems are all excellent test sources for *LISA*, standing out significantly above both the instrument's design sensitivity and the expected average Galactic background signal (although a more rigorous analysis may be needed to predict their exact signal-to-noise ratios; see Stroeer & Vecchio 2006). The estimates for the four bright systems have gone up from initial estimates by Nelemans (2005) due to their rather massive donors, and their relatively low inclinations. The expectations for GP Com remain rather low: it does not stand out from the instrumental and Galactic noise and will be much more difficult to identify. We

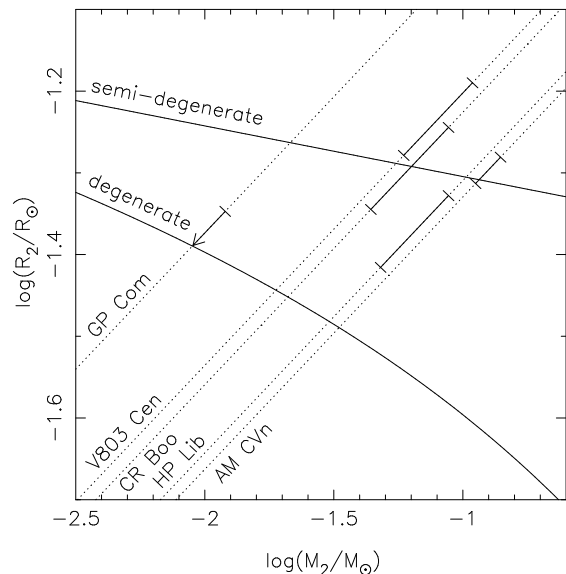


FIG. 2.— Constraints on the masses and radii of the donor stars, compared to degenerate and semi-degenerate evolutionary tracks from Nelemans et al. (2001). The dotted diagonals represent the Roche-lobe filling solutions for the different systems. The solid-line regions represent the constraints on the masses from Table 2. We see that, apart from GP Com, the donors appear to be rather semi-degenerate.

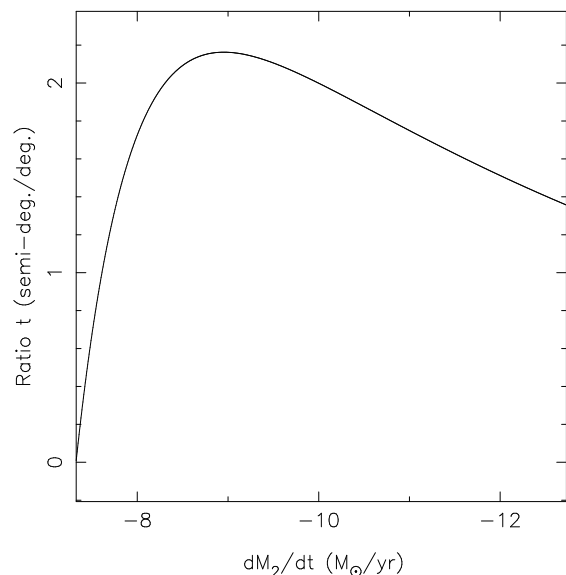


FIG. 3.— Ratio of the integrated times spent at a given mass transfer rate or higher, for a $0.6 M_{\odot}$ white dwarf accreting from a fully degenerate ($0.25 M_{\odot}$) and a semi-degenerate ($0.2 M_{\odot}$) donor star as modeled by Nelemans et al. (2001). Semi-degenerate systems are seen to spend about twice as long at phases of relatively high mass transfer, $10^{-10} \lesssim \dot{M}_2 \lesssim 10^{-8} M_{\odot}/\text{yr}$, corresponding to the mass transfer rates found for AM CVn, HP Lib, CR Boo and V803 Cen.

note that, as long as the uncertainty about the orbital frequency is larger than the frequency resolving power of *LISA* ($\Delta f \sim t_{\text{obs}}^{-1} \sim 10^{-8} \text{ Hz}$, for a mission duration $t_{\text{obs}} = 1 \text{ yr}$), the chances of confusion with Galactic noise sources decrease greatly with more accurately known orbital periods for these systems. The orbital period of AM CVn is known to an accuracy of better than one part

per million from large time-base photometric monitoring

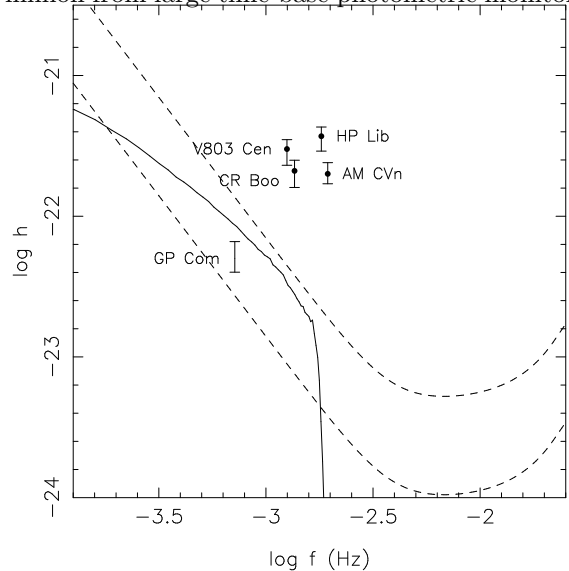


FIG. 4.— Predicted gravitational-wave strain amplitudes h and frequencies f of the five AM CVn stars for which we obtained an *HST* parallax. The upper and lower dashed lines show the design sensitivities of *LISA* for a signal-to-noise ratio of 5 and 1, respectively, in one year of data-collecting (Larson et al. 2000). The solid line is a population synthesis prediction for the confusion-limited Galactic background, also for a mission duration of one year (Nelemans et al. 2004).

($P_{\text{AM CVn}} = 1028.7322 \pm 0.0003 \text{ s}$, Skillman et al. 1999), and the orbital period of HP Lib also seems quite secure ($P_{\text{HP Lib}} = 1102.70 \pm 0.05 \text{ s}$, Patterson et al. 2002), but the orbital periods of especially V803 Cen and CR Boo seem to be less well-known. It would be worthwhile to measure the orbital periods of these systems with greater accuracy.

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APPENDIX

AM CVN AND REFERENCE STAR DATA TABLES

TABLE 3
LOG OF OBSERVATIONS AND FGS PHOTOMETRY

Set	MJD	Roll ($^{\circ}$) ^a	V^b
AM CVn-1	52222.81198	217	14.02 \pm 0.01
AM CVn-2	52225.88485	58	14.01 \pm 0.01
AM CVn-3	52387.43705	217	14.04 \pm 0.02
AM CVn-4	52390.64253	33	14.03 \pm 0.01
AM CVn-5	52431.24828	33	14.03 \pm 0.01
AM CVn-6	52435.52559	58	13.99 \pm 0.01
AM CVn-7	52715.78999	58	14.01 \pm 0.01
AM CVn-8	52719.72357	359	14.04 \pm 0.02
AM CVn-9	52796.35781	359	14.04 \pm 0.02
AM CVn-10	52803.28106	58	14.03 \pm 0.02
CR Boo-1	52095.17132	82	14.51 \pm 0.03
CR Boo-2	52103.46567	82	14.16 \pm 0.01
CR Boo-3	52136.09742	83	14.36 \pm 0.01
CR Boo-4
CR Boo-5	52309.56485	273	13.93 \pm 0.03
CR Boo-6	52322.84773	273	15.99 \pm 0.04
CR Boo-7	52501.29821	83	15.88 \pm 0.04
CR Boo-8	52512.98296	87	15.96 \pm 0.02
CR Boo-9	52676.15807	273	15.61 \pm 0.04
CR Boo-10	52686.69897	273	15.07 \pm 0.01
V803 Cen-1	52112.02035	68	14.19 \pm 0.03
V803 Cen-2	52115.43291	68	13.50 \pm 0.05
V803 Cen-3	52161.84252	37	13.64 \pm 0.01
V803 Cen-4	52164.04853	37	15.68 \pm 0.08
V803 Cen-5	52294.81707	247	13.46 \pm 0.01
V803 Cen-6	52300.82760	247	13.51 \pm 0.01
V803 Cen-7	52526.14146	37	14.64 \pm 0.03
V803 Cen-8	52530.14615	37	13.85 \pm 0.04
V803 Cen-9	52659.74478	246	14.34 \pm 0.02
V803 Cen-10	52664.41432	246	13.69 \pm 0.04
HP Lib-1	52135.63781	74	13.61 \pm 0.03
HP Lib-2	52138.24565	74	13.62 \pm 0.01
HP Lib-3	52168.26915	80	13.59 \pm 0.02
HP Lib-4	52172.41573	80	13.59 \pm 0.02
HP Lib-5	52318.71790	256	13.60 \pm 0.02
HP Lib-6	52326.79246	256	13.60 \pm 0.02
HP Lib-7	52532.15146	80	13.57 \pm 0.02
HP Lib-8	52539.16093	80	13.58 \pm 0.02
HP Lib-9	52680.90353	256	13.56 \pm 0.02
HP Lib-10	52693.71125	256	13.54 \pm 0.02
GP Com-1	52088.34598	65	15.96 \pm 0.01
GP Com-2	52097.16817	65	15.99 \pm 0.01
GP Com-3	52234.70052	229	15.89 \pm 0.02
GP Com-4	52242.04902	229	15.92 \pm 0.01
GP Com-5	52270.97565	245	15.93 \pm 0.01
GP Com-6	52273.91306	245	15.94 \pm 0.02
GP Com-7	52598.75738	229	15.93 \pm 0.02
GP Com-8	52633.85590	244	16.01 \pm 0.02
GP Com-9	52637.92521	244	16.00 \pm 0.02
GP Com-10	52963.80643	229	15.89 \pm 0.01

^a Spacecraft roll as defined in Chapter 2, FGS Instrument Handbook (Nelan & Makidon 2002). ^b Average of 2 to 4 observations at each epoch. Errors are internal and are the standard deviation at each epoch.

TABLE 4
REFERENCE STAR POSITIONS

ID	ξ^a	η^a
AM CVn ^b		
ref-2	−77.5390 0.0003	−137.4972 0.0002
ref-3	159.3017 0.0003	−173.8572 0.0002
ref-5	60.260 0.0003	−88.9279 0.0002
CR Boo ^c		
ref-2	−192.2319 0.0003	−49.5013 0.0002
ref-3	−242.6593 0.0002	−3.4712 0.0001
ref-4	304.3653 0.0003	−16.0044 0.0002
ref-5	250.2984 0.0006	19.8065 0.0004
ref-6	437.8449 0.0009	9.7262 0.0006
V803 Cen ^d		
ref-2	78.2233 0.0003	42.8896 0.0002
ref-3	−119.9175 0.0003	−26.1711 0.0002
ref-4	−55.0075 0.0002	110.9745 0.0002
ref-5	−122.0958 0.0002	67.3278 0.0002
ref-6	137.4346 0.0002	39.0072 0.0002
HP Lib ^e		
ref-2	89.3402 0.0003	−66.1514 0.0002
ref-3	249.1257 0.0003	−18.3677 0.0002
ref-4	9.8453 0.0004	77.8612 0.0003
ref-5	−4.4333 0.0003	55.4678 0.0002
ref-6	−311.6452 0.0003	−13.1930 0.0002
GP Com ^f		
ref-2	81.0209 0.0002	33.9032 0.0001
ref-3	88.3580 0.0002	95.1984 0.0001
ref-4	80.9519 0.0002	−73.6567 0.0001
ref-5	105.5746 0.0003	30.4648 0.0002
ref-6	−103.6979 0.0002	101.5386 0.0002

^a ξ and η are relative RA and Dec in arcseconds^b 12^h34^m54^s.58, +37°37′43″.4, J2000, epoch 2002.44^c 13^h48^m55^s.29, +07°57′34″.8, J2000, epoch 2002.14^d 13^h23^m44^s.51, −41°44′30″.4, J2000, epoch 2002.07^e 15^h35^m53^s.08, −14°13′12″.3, J2000, epoch 2002.14^f 13^h05^m42^s.85, +18°01′02″.6, J2000, epoch 2001.99

TABLE 5
REFERENCE STAR SPECTROPHOTOMETRIC PARALLAXES

ID	Spectral Type	V	M_V	A_V	$m - M$	$\pi_{\text{abs}}(\text{mas})$
AM CVn						
ref-2	G4V	14.37	5.0	0.05	9.4±0.7	1.3±0.4
ref-3	K6V	15.15	7.6	0.05	7.5 0.7	3.2 1.0
ref-5	G4V	12.42	5.0	0.05	7.5 0.7	3.3 1.0
CR Boo						
ref-2	G9V	15.57	5.74	0.02	9.8 0.7	1.1 0.4
ref-3	M2III	11.40	−0.6	0.02	12.0 0.7	0.4 0.1
ref-4 ^a	F2V	6.81	3.0	0.02	3.8 0.7	16.9 0.9
ref-5	G0V	14.82	4.4	0.02	10.4 0.7	0.8 0.3
ref-6	G7V	11.93	5.4	0.02	6.5 0.7	5.1 1.6
V803 Cen						
ref-2	K1V	15.86	6.2	0.31	9.7 0.7	1.3 0.4
ref-3	G4V	15.34	5.0	0.31	10.4 0.7	0.9 0.3
ref-4	F6.5V	13.38	3.8	0.31	9.6 0.7	1.4 0.4
ref-5	G6V	14.17	5.3	0.31	8.9 0.7	1.9 0.6
ref-6	F8V	14.15	4.0	0.31	10.2 0.7	1.1 0.4
HP Lib						
ref-2	F5V	12.86	3.5	0.34	9.4 0.7	1.6 0.5
ref-3	G9V	14.06	5.7	0.34	8.4 0.7	2.6 0.8
ref-4	K7V	12.57	7.9	0.34	4.7 0.7	14.0 4.5
ref-5	K4V	11.80	7.1	0.34	4.7 0.7	13.6 4.4
ref-6	A2.5V	14.60	1.3	0.34	13.3 1.0	0.3 0.1
GP Com						
ref-2	G0V	15.17	4.4	0.02	10.8 0.7	0.7 0.2
ref-3	G8V	14.39	5.58	0.02	8.8 0.7	1.7 0.6
ref-4	K0V	14.25	5.58	0.02	8.7 0.7	1.8 0.6
ref-5	K5V	13.56	7.4	0.02	6.2 0.7	5.7 1.9
ref-6	G8V	15.12	5.58	0.02	9.5 0.7	1.2 0.4

^a = HIP 67379

TABLE 6
FGS AND NEAR-IR REFERENCE STAR PHOTOMETRY

ID	V	K	$J - H$	$J - K$	$V - K$
AM CVn					
ref-2	14.37 0.1	12.79 0.03	0.44 0.04	0.43 0.03	1.58 0.10
ref-3	15.15 0.1	12.09 0.02	0.74 0.04	0.82 0.03	3.06 0.10
ref-5	12.42 0.1	10.88 0.02	0.41 0.04	0.42 0.03	1.54 0.10
CR Boo					
ref-2	15.57 0.1	13.64 0.05	0.47 0.05	0.48 0.05	1.93 0.11
ref-3	11.4 0.1	7.13 0.05	0.91 0.02	1.13 0.05	4.28 0.11
ref-4	14.8 0.1	5.93 0.01	0.21 0.04	0.22 0.02	0.87 0.05
ref-5	6.8 0.1	13.54 0.05	0.34 0.05	0.27 0.06	1.46 0.11
ref-6	11.89 0.1
V803 Cen					
ref-2	15.86 0.1	13.42 0.04	0.53 0.04	0.62 0.04	2.44 0.11
ref-3	15.34 0.1	13.58 0.04	0.45 0.04	0.43 0.05	1.76 0.11
ref-4	13.38 0.1	11.96 0.02	0.29 0.03	0.33 0.03	1.42 0.10
ref-5	14.17 0.1	12.29 0.02	0.42 0.03	0.51 0.03	1.88 0.10
ref-6	14.15 0.1	12.45 0.03	0.35 0.03	0.36 0.04	1.70 0.10
HP Lib					
ref-2	12.88 0.1	11.40 0.02	0.30 0.03	0.34 0.03	1.48 0.10
ref-3	14.11 0.1	11.93 0.02	0.51 0.03	0.51 0.03	2.18 0.10
ref-4	12.6 0.1	9.17 0.02	0.69 0.03	0.84 0.03	3.43 0.10
ref-5	11.84 0.1	8.87 0.02	0.66 0.03	0.77 0.03	2.97 0.10
ref-6	14.6 0.1
GP Com					
ref-2	15.17 0.1	13.73 0.05	0.34 0.04	0.36 0.06	1.44 0.11
ref-3	14.39 0.1	12.62 0.03	0.43 0.03	0.46 0.03	1.77 0.10
ref-4	14.25 0.1	12.24 0.03	0.46 0.03	0.54 0.03	2.01 0.10
ref-5	13.56 0.1	10.71 0.02	0.67 0.02	0.74 0.03	2.85 0.10
ref-6	15.12 0.1	13.44 0.04	0.40 0.04	0.53 0.05	1.68 0.11

TABLE 7
FIELD A_V FROM REFERENCE STAR SPECTROPHOTOMETRY

ID	Spectral Type	$(V - K)_0$	$V - K$	$E(V - K)$	A_V^a	$\langle A_V \rangle$
AM CVn						0.05±0.02
ref-2	G4V	1.52	1.58	0.06	0.07	
ref-3	K6V	3.01	3.06	0.05	0.06	
ref-5	G4V	1.52	1.54	0.02	0.02	
CR Boo						0.03±0.04
ref-2	G9V	1.88	1.93	0.05	0.05	
ref-3	M2III	4.30	4.28	-0.02	-0.02	
ref-4	F2V	0.86	0.87	0.01	0.01	
ref-5	G0V	1.41	1.46	0.05	0.06	
V803 Cen						0.31±0.09
ref-2	K1V	2.14	2.44	0.30	0.33	
ref-3	G4V	1.52	1.76	0.24	0.26	
ref-4	F6.5V	1.19	1.42	0.23	0.26	
ref-5	G6V	1.67	1.88	0.21	0.23	
ref-6	F8V	1.28	1.70	0.42	0.46	
HP Lib						0.34±0.06
ref-2	F5V	1.10	1.48	0.38	0.42	
ref-3	G9V	1.88	2.18	0.3	0.33	
ref-4	K7V	3.17	3.43	0.26	0.29	
ref-5	K4V	2.68	2.97	0.29	0.32	
GP Com						0.02±0.11
ref-2	G0V	1.41	1.44	0.03	0.03	
ref-3	G8V	1.80	1.77	-0.03	-0.03	
ref-4	K0V	1.96	2.01	0.05	0.05	
ref-5	K5V	2.70	2.85	0.15	0.16	
ref-6	G8V	1.80	1.68	-0.12	-0.14	

^a $A_V = 1.1E(V - K)$